

Possibility of Bending-Induced Fracture in Curved Double-Clad Fibers

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Abstract: Rare-earth-doped optical fibers are one of the most promising solid-state lasers. In these fiber lasers, a cladding-pumping scheme using large-mode-area double-clad fibers (DCFs) is utilized to increase the overall conversion efficiency of pumping light and to overcome the restriction owing to the onset of stimulated Raman scattering. On the other hand, it is extremely challenging to increase the fiber core size while retaining the excellent beam quality because fibers with large core size allow propagation of several higher-order modes (HOMs), except for the fundamental mode (FM). In order to suppress HOMs, DCFs are bent with a relatively small bend radius. For the bent DCFs, the fracture behavior, including delayed fracture, was investigated on the basis of the fracture mechanics concept. When a bent DCF is subjected to a high applied stress, failure occurs by the extension of a crack from the surface of the inner cladding (silica glass) layer of the DCF. When DCFs with core diameters of 20 and 40 μm were curved to be stored in the apparatus to maintain large bending radii of > 245 and 275 mm, respectively, it was found that both instantaneous and delayed fracture of bent DCFs could not occur in either air or distilled water. When a DCF is homogeneously curved in air and in water, bending loss occurs in the core and the optical power lost in the core is emitted from the outer interface (or boundary) between the inner cladding (silica glass) and outer cladding (low-index polymer) layers. As the transmittance of the polymer is not 100%, the leaked light is absorbed and heat accumulates in the polymer. The heat generated in the polymer through the absorption of optical power is transferred to the neighboring cladding (silica glass) layer. When the temperature of the outer wall of the cladding layer is higher than that of the inner wall, tensile stress is generated on the inner wall and compressive stress is generated on the outer wall. The thermal stress generated on the inner wall was estimated. It was concluded that the instantaneous fracture of curved DCFs could not occur in air or in distilled water under high-power laser operation.

Keywords: Double-Clad Fiber, Bending, Fracture Strength, Time to Failure, Fracture Mechanics

1. Introduction

Rare-earth-doped optical fibers are one of the most promising solid-state lasers for efficient diode-pumped high-power continuous-wave (CW) laser systems and fiber chirped-pulse amplification (CPA) systems. The output power from the ytterbium (Yb)-doped fiber lasers has abruptly increased over the past decade [1-6]. High conversion efficiencies from pump light are obtained in Yb-doped double-clad fibers (DCFs) by using a cladding-pumping scheme [7] to ensure that virtually all of the incident pump power is absorbed in the doped fiber core.

To overcome the restriction owing to the onset of stimulated Raman scattering (SRS), low-numerical-aperture (NA)

large-mode-area (LMA) fibers [8] are utilized as DCFs. Typical LMA fibers used in the CW laser operation have core diameters of 20-40 μm and NA of < 0.09 [9-14]. A high output power of > 200 W in the CW laser operation using cladding-pumped Yb-doped and/or Nd+Yb-codoped LMA fibers [9-24] has been reported.

On the other hand, it is extremely challenging to increase the fiber core size while retaining an excellent beam quality because fibers with large core sizes allow propagation of several higher order mode (HOM), except for the fundamental mode (FM). In order to suppress HOMs, DCFs are bent with a relatively small bend radius [13, 14, 24].

It is well known that failures at bends in an optical fiber are caused by light leaking from the core when the fiber is

accidentally bent tightly with a high power input [25-33]. Two failure regimes have been classified by Sikora *et al.*, which they named regime 1 (R1) and regime 2 (R2) failures [27]. Among them, R1 failure will lead to the catastrophic failure of the fiber and the burning of the coating [28, 33]. In the previous paper [34], we clarified allowable curvature radii of the bent DCFs which were necessary to prevent the R1 failure and/or the generation of fiber fuse phenomenon under high-power laser operation.

The stress distribution in the straight DCF was studied by Brown and Hoffman to estimate the radially varying index of refraction due to the stress-optic effect [35]. They also calculated the maximum tolerable heat power per unit length using the tensile-limited stress for the DCF. Zervas investigated the power limiting factor of high-power fiber amplifiers using a failure-in-time analysis [36]. However, the possibility of fracture in the bent DCF is not clear at the moment. In this article, the fracture behavior, including delayed fracture, of the bent DCFs was investigated on the basis of the fracture mechanics concept.

2. Fracture Behavior in Curved DCF

When optical fibers are fabricated with the fiber drawing apparatus, it is very difficult to produce a long defect-free fiber. It should be noted that the existence of a small crack on the surface is always taken into account in the determination of the critical safe stress applicable to a fiber without breakage.

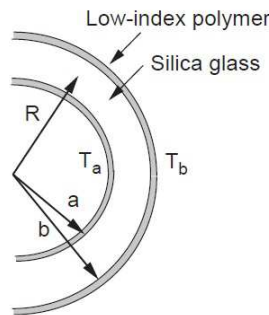


Figure 1. Schematic of curved DCF.

When a DCF is homogeneously curved with the bending radius R , as shown in Figure 1, tensile stress is generated on the outer wall ($r = b$) and a compressive stress is generated on the inner wall ($r = a$). Since most glass materials are more resistant to compression than to tension, it is expected that the surface of the outer wall will be susceptible to fracture owing to the presence of tensile stress.

The tensile stress at $r = b$ is given by

$$\sigma = \frac{E(b-R)}{R} \quad (1)$$

where E ($= 73$ GPa) is Young's modulus of the silica glass.

The relationships between R and σ in the bent DCF was investigated using Eq. (1). The calculated result is shown in Figure 2. In the calculation, the diameter ($2r_1$) of the inner cladding layer of the DCF was assumed to be $400 \mu\text{m}$, which

leads to $b - R = 200 \mu\text{m}$.

The inert strength σ_{IC} of $5,670$ MPa has been reported for silica optical fibers [37]. As shown in Figure 2, σ decreases rapidly with increasing R and becomes smaller than σ_{IC} at $R \geq 3$ mm. For $R = 100$ - 300 mm, the corresponding σ values are listed in Table 1.

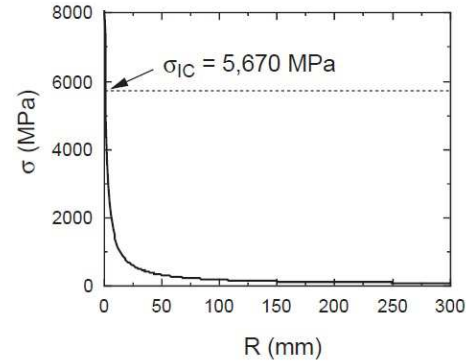


Figure 2. Tensile stress on outer wall versus curvature radius in bent DCF.

Table 1. Tensile stress against curvature radius.

R (mm)	σ (MPa)
100	146
150	97
200	73
250	58
300	49

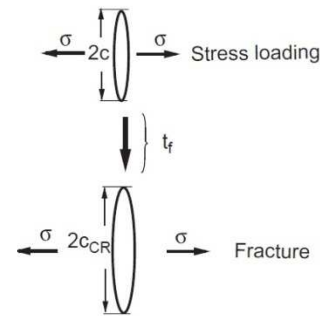


Figure 3. Fracture in DCF.

When a bent DCF is subjected to a high applied stress (σ), failure occurs by the extension of a crack from the surface of the inner cladding (silica glass) layer of the DCF. A crack with an initial size of $2c$ grows until it reaches a critical size $2c_{CR}$ after the passage of the time to failure t_f . When c becomes c_{CR} , the part of the cladding layer, in which the crack exists on the surface, fails almost instantaneously, as shown in Figure 3.

On the other hand, if the applied stress is reduced, a time delay is observed between the time of first exposure to stress and the time of failure. This phenomenon is called “delayed failure”.

In the following, the fracture for which t_f is very short (< 1 s), is referred to as “instantaneous fracture” in order to distinguish the fracture patterns.

In the next section, the fracture strength of the bent DCFs, which is an important parameter in the instantaneous fracture, is estimated.

3. Fracture Strength of Curved DCF

It is assumed that an internal crack (flaw) with a half-length of c exists on the fiber surface perpendicular to the fiber axis and c is fairly small compared with the fiber diameter.

The critical stress intensity factor K_{IC} at the crack front is approximately given by [38]

$$K_{IC} = \frac{2.2}{\sqrt{c}} \sigma_f \sqrt{c} \equiv Y \sigma_f \sqrt{c} \quad (2)$$

where Y is a geometric constant and σ_f is the tensile fracture strength acting on the fiber surface. The K_{IC} values of 0.75-0.87 MPa m^{1/2} [38-41] have been reported for conventional optical fibers in air.

On the other hand, the water immersion of DCFs is performed to remove heat efficiently from the fiber surface [11]. K_{IC} for the fiber in distilled water is estimated to be about 0.37 MPa m^{1/2} [38], which is about half that in air.

The relationships between c and σ_f in air and in distilled water were investigated using Eq. (2). The calculated results are shown in Figure 4. In the calculation, K_{IC} values of 0.75 and 0.37 MPa m^{1/2} were used for the estimation of σ_f in air and in water, respectively. As shown in Figure 4, σ_f decreases rapidly with increasing c . For example, if a fiber contains a flaw with c of 10 μ m on the surface, σ_f is estimated to be 191 MPa in air and 94 MPa in water.

On the other hand, the inert strength σ_{IC} (5,670 MPa) corresponds to σ_f in air when the flaw size c is about 0.01 μ m.

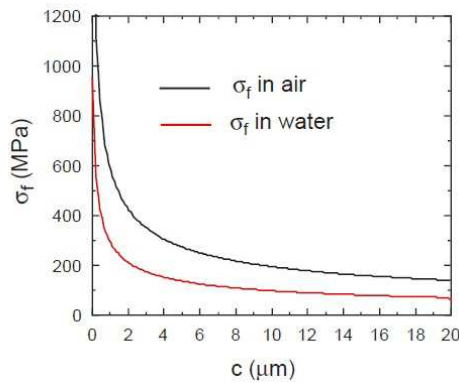


Figure 4. Fracture strength in air and/or in distilled water versus half-length of flaw on fiber surface.

For flaw size $c = 1$ -20 μ m, the corresponding σ_f values are listed in Table 2.

Table 2. Fracture strength against flaw size.

c (μ m)	σ_f (MPa) in air	σ_f (Mpa) in water
1	604	298
2	427	211
5	270	133
10	191	94
15	156	77
20	135	67

As the typical crack size c of the conventional optical fiber is 1 μ m or less [38] and the c of the glass is normally less

than 10 μ m [42], we can expect c on the inner cladding surface of the DCF to be slightly large (1-10 μ m) compared with that of a conventional optical fiber. It was recommended for DCFs with core diameters of 20 and 40 μ m being curved for storage in the apparatus to maintain large R values of > 245 and 275 mm, respectively, for high-power laser operation [34]. As shown in Table 1, tensile stresses of 50-60 MPa occur on the outer wall ($r = b$) when R is about 250-300 mm. These tensile stresses are smaller than the fracture strengths both in air and in water when c on the inner cladding surface of the DCF is 1-10 μ m (see Table 2).

Therefore, it is concluded that when DCFs with core diameters of 20 and 40 μ m are curved to be stored in the apparatus to maintain large R values of > 245 and 275 mm, respectively, instantaneous fracture does not occur in the bent DCFs.

In the next section, the time to failure, t_f , of the DCF is estimated, which is an important parameter in the delayed fracture.

4. Time to Failure of Curved DCF

The typical crack size c of the conventional optical fiber has a small value of 1 μ m or less [38]. This was achieved by conducting a proof test [43, 44]. The samples of weaker fiber are eliminated during the proof test. The proof-test stress σ_p corresponds to the largest flaw size possible in the tested fiber, since any larger flaws would cause failure during the proof test.

On the other hand, the largest crack size on the inner cladding surface of the DCF is unknown, but it can be considered to be slightly large (1-10 μ m), compared with that on a conventional optical fiber. Therefore, it was assumed that the fracture strength σ_f at $c = 10$ μ m was used instead of σ_p in the estimation of the minimum time to failure, t_{min} , of the bent DCF.

For many glass and ceramic materials, the subcritical crack growth rate at a constant stress is described as a power function of the stress intensity factor K as [43, 45, 46]

$$\frac{dc}{dt} = AK^N, \quad (3)$$

where A and N are constants. It is well known that there is relationship between parameter A and the water vapor pressure [46] and the chemical interaction between strained crack-tip bonds in the silica glass and water molecules from the environment [47]. The subcritical crack growth process is thermally activated, and the existence of water molecules on the surface results in the lowering of the activation energy of this process [48]. As a result, the A value estimated in distilled water tends to be larger than that in air. Sawaki *et al.* found that the A value estimated in distilled water at 22°C was about 3.5 times that in air at 24°C [38].

t_{min} under a constant stress σ_a can be derived using the proof stress σ_p as [49]

$$t_{min} = B \sigma_a^{-N} \sigma_p^{N-2}, \quad (4)$$

where

$$B = \frac{2}{AY^2(N-2)K_{IC}^{N-2}}, \quad (5)$$

with K_{IC} being a critical stress intensity factor and Y a geometric constant.

The subcritical crack growth parameters N and B in air can be estimated to be 22.23 and $1.56 \times 10^6 \text{ MPa}^2 \text{ s}$, respectively, from dynamic fatigue tests of optical glass fibers [37]. In distilled water, B has been estimated to be $7.19 \times 10^{11} \text{ MPa}^2 \text{ s}$ by using $K_{IC} (= 0.37 \text{ MPa m}^{1/2})$ in water, which is about half that ($0.75 \text{ MPa m}^{1/2}$) in air, and parameter A in water, which is about 3.5 times that in air [38].

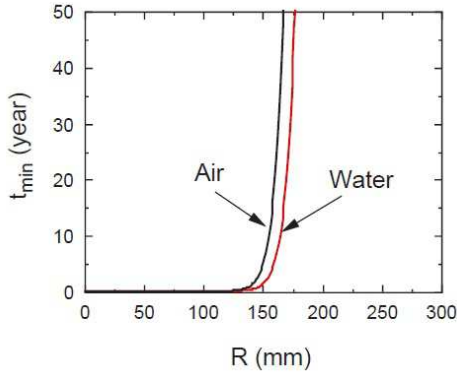


Figure 5. Minimum time to failure in air and/or in distilled water versus curvature radius of bent DCF.

The relationships between t_{\min} and R in air and in distilled water were investigated using Eq. (1) and (4). The calculated results are shown in Figure 5. In the calculation, σ_p values of 191 and 94 MPa were used for the estimation of t_{\min} in air and in water, respectively. As shown in Figure 5, the t_{\min} values in air and in distilled water increase rapidly at $R > 150$ mm, and $t_{\min} \geq 10$ years is obtained at $R \geq 173$ mm in air and $R \geq 184$ mm in distilled water.

Therefore, it is concluded that the delayed fracture of bent DCFs cannot occur in either air or distilled water when DCFs with core diameters of 20 and 40 μm are curved to be stored in the apparatus to maintain large R values of > 245 and 275 mm, respectively.

In the next section, the thermal stresses occurred in the bent DCFs are investigated in the case of temperature of the outer wall, T_b , being larger than that of the inner wall, T_a .

5. Thermal Stress in Curved DCF

When a DCF is homogeneously curved with the bending radius R , as shown in Figure 1, bending loss occurs in the core and the optical power lost in the core is emitted from the outer interface (or boundary) between the inner cladding (silica glass) and outer cladding (low-index polymer) layers [34]. As the transmittance of the polymer is not 100%, the leaked light is absorbed and heat accumulates in the polymer.

The heat generated in the low-index polymer through the absorption of optical power is transferred to the neighboring cladding (silica glass) layer, as shown in Figure 6.

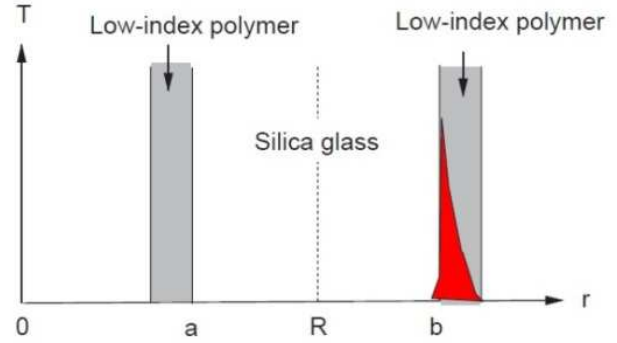


Figure 6. Schematic of temperature distribution in curved DCF.

A bent DCF can be modeled as a hollow disk, as shown in Figure 1, on the basis of the assumption that there is no temperature gradient in the plate thickness direction. When an axially symmetric temperature distribution $T = T(r)$ is given to the hollow silica glass disk, the radial thermal stress σ_r , the tangential thermal stress σ_ϕ , and the axial (z) thermal stress σ_z are given as [50]

$$\sigma_r = \frac{\alpha E}{r^2} \left[\frac{r^2 - a^2}{b^2 - a^2} \int_a^b T r dr - \int_a^r T r dr \right], \quad (6)$$

$$\sigma_\phi = \frac{\alpha E}{r^2} \left[\frac{r^2 + a^2}{b^2 - a^2} \int_a^b T r dr + \int_a^r T r dr - T r^2 \right], \quad (7)$$

$$\sigma_z = 0, \quad (8)$$

where it is assumed that the axial end faces are free of traction. In Eq. (6) and (7), $\alpha (= 0.55 \times 10^{-6} \text{ K}^{-1})$ [39] is the thermal expansion coefficient of the silica glass.

The temperature distribution for steady heat conduction is given by

$$T = T_a + (T_b - T_a) \ln(r/a) / \ln(b/a). \quad (9)$$

Substituting Eq. (9) into Eq. (6) and (7), the steady thermal stresses of the bent DCF become the following equations:

$$\sigma_r = \frac{\alpha E(T_a - T_b)}{2 \ln(b/a)} \left[-\ln\left(\frac{b}{r}\right) + \frac{a^2}{b^2 - a^2} \left(\frac{b^2}{r^2} - 1 \right) \ln(b/a) \right], \quad (10)$$

$$\sigma_\phi = \frac{\alpha E(T_a - T_b)}{2 \ln(b/a)} \left[1 - \ln\left(\frac{b}{r}\right) - \frac{a^2}{b^2 - a^2} \left(\frac{b^2}{r^2} + 1 \right) \ln(b/a) \right]. \quad (11)$$

The thermal stresses generated on the inner ($r = a$) and outer ($r = b$) walls are given by the following equations:

$$(\sigma_r)_{r=a} = (\sigma_r)_{r=b} = 0, \quad (12)$$

$$(\sigma_\phi)_{r=a} = \frac{\alpha E(T_b - T_a)}{2} \left[\frac{2b^2}{b^2 - a^2} - \frac{1}{\ln(b/a)} \right], \quad (13)$$

$$(\sigma_\phi)_{r=b} = \frac{\alpha E(T_a - T_b)}{2} \left[-\frac{2a^2}{b^2 - a^2} + \frac{1}{\ln(b/a)} \right]. \quad (14)$$

When a DCF with an inner cladding radius r_1 of 200 μm is homogeneously curved with the bending radius R , a and b are given by $R - 200 \mu\text{m}$ and $R + 200 \mu\text{m}$, respectively. In this case, the following approximation is valid for $R > 5$ mm.

$$\left[\frac{2b^2}{b^2 - a^2} - \frac{1}{\ln(b/a)} \right] \approx \left[-\frac{2a^2}{b^2 - a^2} + \frac{1}{\ln(b/a)} \right] \approx 1. \quad (15)$$

When the temperature of the outer wall ($r = b$) is higher than that of the inner wall ($r = a$), as shown in Figure 6, tensile stress is generated on the inner wall and compressive stress is generated on the outer wall.

As described above, when a DCF is homogeneously curved with the bending radius R , tensile stress is generated on the outer wall ($r = b$) and compressive stress is generated on the inner wall ($r = a$). Therefore, the thermally induced tensile stress at the inner wall is lowered by the bending-induced compressive stress. The tensile stress generated on the inner wall ($r = a$) is given by the following equation:

$$(\sigma_{\phi})_{r=a} \approx \frac{\alpha E(T_b - T_a)}{2} + \frac{E(a-R)}{R} \quad (16)$$

The relationships between $(\sigma_{\phi})_{r=a}$ and T_b of the bent DCF on the cases of $R = 200$ and 300 mm were investigated using Eq. (16). The calculated results are shown in Figure 7.

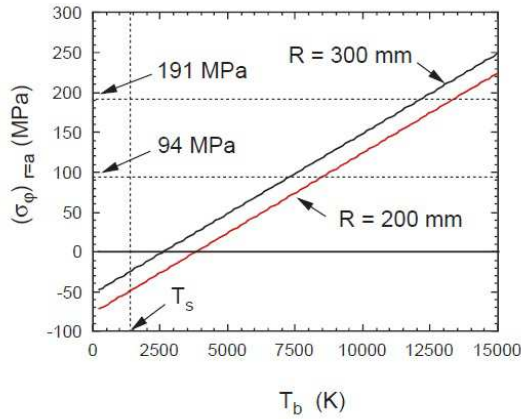


Figure 7. Tensile stress at inner wall versus temperature of outer wall in bent DCF.

As shown in Figure 7, $(\sigma_{\phi})_{r=a}$ increases with increasing T_b .

The values of 191 and 94 MPa are the fracture strengths in air and in water at $c = 10 \mu\text{m}$, as shown in Table 2. $(\sigma_{\phi})_{r=a}$ goes up to 191 MPa when T_b becomes 12,240 K or 13,450 K at $R = 300$ or 200 mm, respectively. Similarly $(\sigma_{\phi})_{r=a}$ goes up to 94 MPa when T_b becomes 7,400 K or 8,620 K at $R = 300$ or 200 mm, respectively.

These temperatures of 7,400-13,450 K are extremely high compared with the softening temperature T_s ($= 1,373$ K [27, 28]) of the silica glass. When the temperature at the heating part ($r = b$) of the silica glass exceeds T_s , the glass at the heating part will begin to deform and the compressive stress at this part will relax and disappear. The tensile stress at $r = a$ will be inhibited from increasing when T_b reaches T_s .

The values of $(\sigma_{\phi})_{r=a}$ at $T_b = T_s$ are about -27 and -51 MPa at $R = 300$ and 200 mm, respectively (see Figure 7). These are compressive stresses, not tensile stresses.

It was recommended for DCFs with core diameters of 20 and 40 μm being curved for storage in the apparatus to maintain large R values of > 245 and 275 mm, respectively, for high-power laser operation [34]. As described above, no

tensile stresses occur on the inner wall ($r = a$) when R is 200-300 mm.

Instantaneous fracture occurs due to the tensile stresses larger than the fracture strengths both in air and in water when c on the inner cladding surface of the DCF is 1-10 μm .

Therefore, it is concluded that when DCFs with core diameters of 20 and 40 μm are curved to be stored in the apparatus to maintain large R values of > 245 and 275 mm, respectively, instantaneous fracture does not occur in air or in distilled water under high-power laser operation.

6. Conclusion

For the bent DCFs, the fracture behavior, including delayed fracture, was investigated on the basis of the fracture mechanics concept. When a bent DCF was subjected to a high applied stress, failure occurred by the extension of a crack from the surface of the inner cladding (silica glass) layer of the DCF. When DCFs with core diameters of 20 and 40 μm were curved to be stored in the apparatus to maintain large bending radii of > 245 and 275 mm, respectively, it was found that both instantaneous and delayed fracture of bent DCFs could not occur in either air or distilled water. When a DCF is homogeneously curved in air and in water, bending loss occurs in the core and the optical power lost in the core is emitted from the outer interface (or boundary) between the inner cladding (silica glass) and outer cladding (low-index polymer) layers. As the transmittance of the polymer is not 100%, the leaked light is absorbed and heat accumulates in the polymer. The heat generated in the polymer through the absorption of optical power is transferred to the neighboring cladding (silica glass) layer. When the temperature of the outer wall of the cladding layer is higher than that of the inner wall, tensile stress is generated on the inner wall and compressive stress is generated on the outer wall. These thermal stress generated on the inner wall was estimated. It was concluded that the instantaneous fracture of curved DCFs could not occur in air or in distilled water under high-power laser operation up to 10 kW.

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